

APPLICATION OF COMPOSITE FRACTURE MECHANICS TO BONE FRACTURE ANALYSIS USING ABAQUS XFEM

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Introduction

Bone Fracture

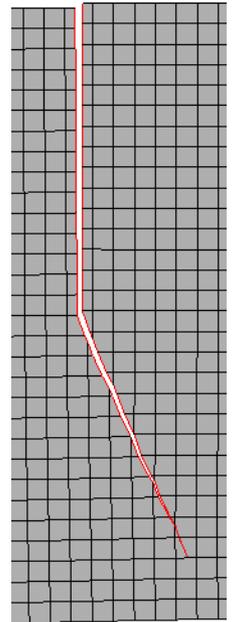
- **Predicting and preventing bone fractures is an important topic in orthopedics**
 - High rate of incidences
 - e.g.: 1.66 million hip fracture world-wide in 1990
 - Result in serious complications
 - e.g.: infections and nonunion
 - The impact is more severe for elderly
 - Loss of mobility and independence
 - Blood clots may develop
 - Understanding the fracture behavior of bone will help researchers find proper **bone strengthening treatment**
 - To prevent such traumatic failure



Introduction

Abaqus XFEM

- Finite element analysis has been instrumental in understanding various aspects of bone mechanics
- Modelling bone fracture had been difficult with traditional FEA
 - The crack propagation path had to be defined before the analysis
 - The finite element mesh had to conform to geometric discontinuities
- Abaqus introduced eXtended Finite Element Method (XFEM) from version 6.9
 - Permits a crack to be located in the **element interior**
 - The crack location is **independent of the mesh**
 - Simulate initiation and propagation of a discrete crack along **an arbitrary, solution-dependent path** without the requirement of remeshing in the bulk materials



Introduction

Abaqus XFEM

- **Damage initiation criteria**

- Built-in criteria

- Maximum principal stress
- Maximum principal strain
- Maximum nominal stress
- Maximum nominal strain
- Quadratic nominal stress
- Quadratic nominal strain

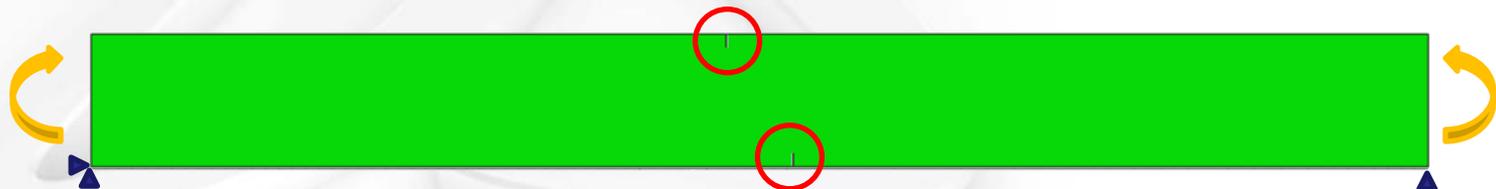
- **User-defined damage initiation criterion** (available in 6.10EF)

- Provides users with access to the **damage initiation criterion** and the **direction of the crack propagation**
- Allows the specification of competing failure mechanisms
 - **Multiple crack initiation mechanisms** in composite material
- Great tool to study bone fracture properties
 - Which failure criterion best predicts when a crack will initiate

Methods

Example 1: Beam Bending

- **Objective**
 - Demonstrate effect of different damage initiation criteria on a simple model
- **FEA model**
 - 2D plane strain elements
 - Linear elastic material
 - Pure bending loading conditions applied
- **XFEM**
 - Two initial cracks of the same size placed in both tension and compression side
 - Three damage initiation criteria analyzed
 - Built-in maximum principal stress criterion
 - User-defined compressive only damage initiation criterion
 - User-defined combined tension and compression damage criteria



Methods

Example 2: Mode II Fracture of Cortical Bone

- **Objective**

- Demonstrate how composite fracture criteria could be applied to predict cortical bone fracture using XFEM and user defined damage initiation criteria

- **FEA model**

- 3D model of a notched bone under asymmetric four point bending
- Assuming fiber runs along the axis of the specimen

- **XFEM**

- Two damage initiation criteria analyzed
 - Built-in maximum principal stress criterion
 - Composite fracture criterion with two competing failure mechanisms



Methods

Example 2: Mode II Fracture of Cortical Bone

● Fiber failure mechanism

- The fiber direction is based on the material orientation

- Fiber failure stresses:

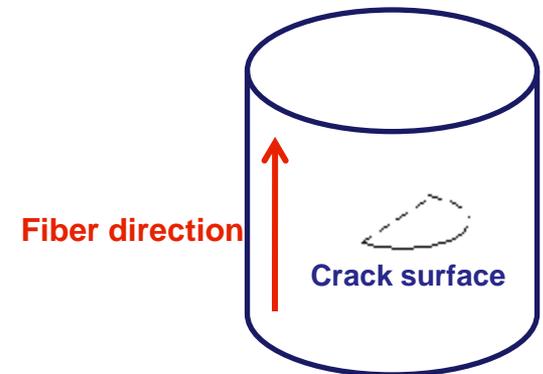
$$\sigma_f = 133 \text{ MPa}$$

$$\tau_f = 68 \text{ MPa}$$

- Fiber failure criterion

$$\bar{\sigma} = \sqrt{\frac{\sigma_{11}^2}{\sigma_f^2} + \frac{\tau_{12}^2}{\tau_f^2} + \frac{\tau_{13}^2}{\tau_f^2}} \geq 1$$

- Crack surface is always perpendicular to the fiber direction



Methods

Example 2: Mode II Fracture of Cortical Bone

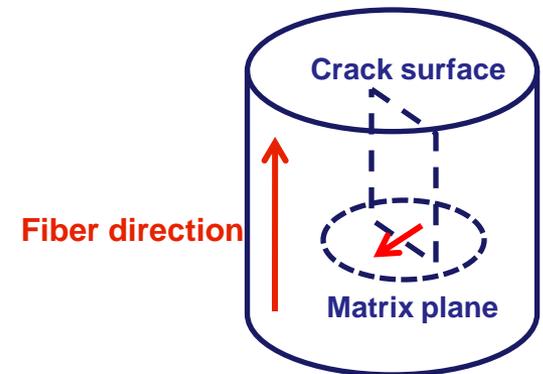
● Matrix failure mechanism

- Matrix plane: any plane perpendicular to the fiber direction
- The in-plane maximum principal stress and its direction within the matrix plane is used to determine the crack initiation and propagation direction

- Matrix failure stress:

$$\sigma_f = 51 \text{ MPa}$$

- Crack surface is the plane that perpendicular to the maximum in-plane principal direction and parallel to the fiber direction



Methods

Example 3: Femur Fracture

- **Objective**

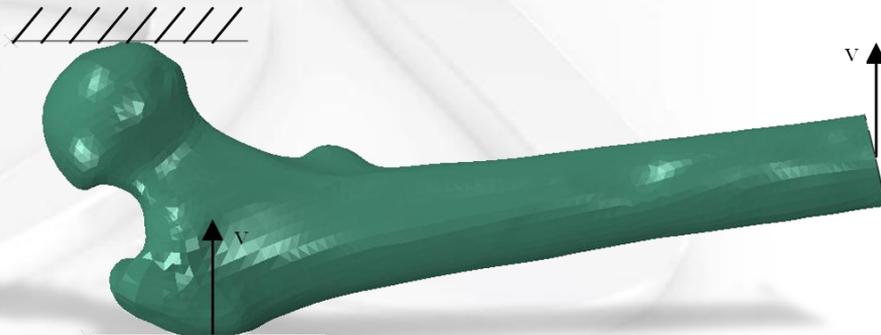
- Demonstrate how user-defined damage criteria could be applied to whole bone fracture simulation

- **FEA model**

- A femur fracture test is simulated
- Apparent bone density implemented as a field variable
- Bone elastic and damage properties defined as functions of bone density through field variable dependent material properties

- **XFEM**

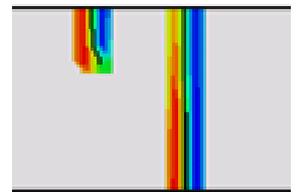
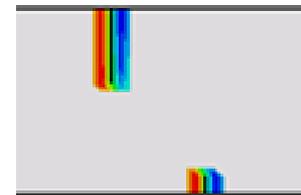
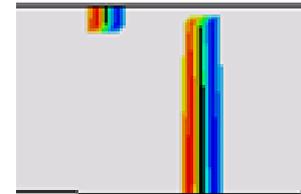
- Two damage initiation criteria analyzed
 - Built-in maximum principal strain criterion
 - User-defined combined tension and compression damage criteria



Results

Example 1: Beam Bending

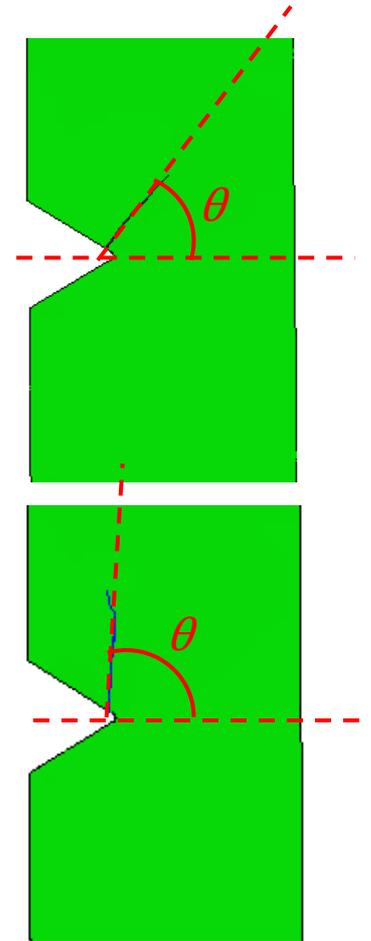
- **Built-in maximum principal stress criterion**
 - Only crack on the tension side propagated
- **User-defined compressive only damage initiation criterion**
 - Only crack on the compressive side propagated
 - Crack propagation stopped at neutral axis due to the stabilizing effect of contact at the crack surfaces
- **User-defined combined tension and compression damage criteria**
 - Both cracks propagated
 - Crack on the compressive side stopped at neutral axis



Results

Example 2: Mode II Fracture of Cortical Bone

- **Built-in maximum principal stress criterion**
 - Crack deflection angle $\theta \sim 65^\circ$
 - Close to analytical solution
- **Composite fracture criterion**
 - Crack deflection angle $\theta \sim 90^\circ$
 - Similar results were observed in experimental study on human cortical bone fracture¹

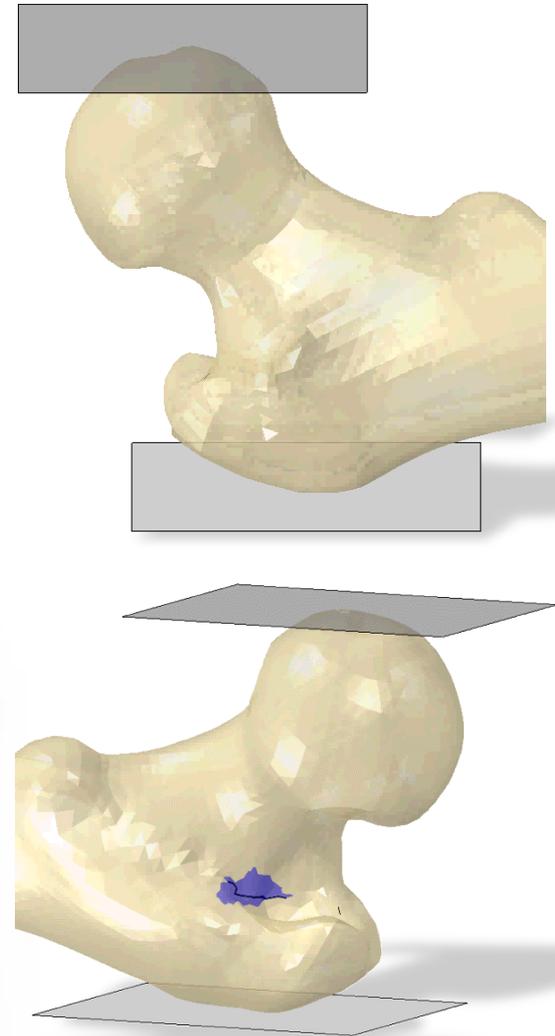


1. Zimmermann, et al. "Mixed-mode Fracture of Human Cortical Bone, Biomaterial, 2009, 30: 5877-5884

Results

Example 3: Femur Fracture

- **Built-in maximum principal strain criterion**
 - Crack initiated from posterior side of the femur neck
 - Right underneath the femur head
 - Crack propagated mostly along the surface
 - Did not extend deep into the femur neck
- **User-defined combined tension and compression damage criteria**
 - Crack initiated from the anterior side of the femur neck
 - Next to the greater trochanter
 - Crack propagated along the surface and into the femur neck



Summary

Abaqus XFEM for Bone Fracture Study

- **Bone is a very complex material**
 - Hierarchical: multilevel structure complexity
 - Inhomogeneous: material property varies spatially
 - Orthotropic: stronger in the load carrying direction
 - Asymmetric: stronger in compression than in tension and shear
 - Living tissue that is capable of repairing and remodelling itself
- **Fracture mechanics property is one of the most important aspects of bone that concerns millions of people's wellbeing**
 - It is not yet fully understood
 - Abaqus XFEM is another unique powerful tool for researchers to:
 - Better understand bone fracture and failure behavior
 - Develop strengthening treatment